

Math 252

Exam I

---

Name

"In mathematics you don't  
understand things. You just get  
used to them."

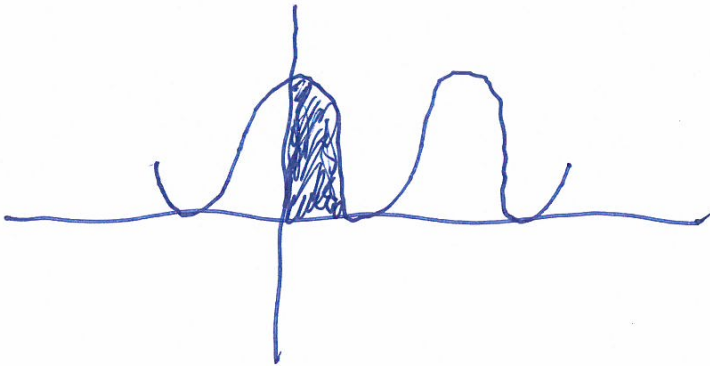
--Johann von Neuman

THIS EXAM IS OPEN BOOK AND OPEN NOTES BUT ALL ELECTRONICS  
MUST BE TURNED OFF AND PUT AWAY (THIS INCLUDES CELL-PHONES  
AND I-PADS). BALD ANSWERS ARE NOT ALLOWED ON ANY  
QUESTION.

1 (10 Points). Evaluate  $\int \cos(x) \sin(2x) dx$ .

2 (12 Points). Evaluate  $\int_0^4 \frac{dx}{\sqrt{4-x}}$

3 (14 Points). Consider the graph of  $y=1+\cos(x)$ , as shown. Compute the volume of the shaded region when rotated about the x-axis.



4 (13 Points). A region in the  $xy$ -plane is bounded by the  $x$ -axis and the line  $y = x^2 - 4$ . A solid object sits on this region. Cross sections perpendicular to the  $x$ -axis are squares. What is the volume of this object?

5 (13 Points). A force of two pounds stretches a spring two inches. How much work is required to stretch the spring two feet? Express your answer in foot-pounds.

6 (14 Points). Evaluate  $\int \frac{8x^3}{\sqrt{9-x^2}} dx$  using a trig-substitution.

8 (13 Points). Consider the graph of  $y=7+6x^{1.5}$  on the interval  $0 \leq x \leq 1$ .  
What is the arc-length?