

In **30 minutes** do the following problems, **without help** from any references, computing devices, or people. Write your solutions on either a printout or blank paper. If you use blank paper, do the problems on **1 sheet of paper, in the order given**. Upload a pdf of your solutions to **Gradescope, by midnight**.

Show your work.

1.

- (a) Using the definition, find the Taylor series for the function $f(x) = \sqrt{x}$ at $a = 4$, writing out at least the first 4 terms.

- (b) Use the 2nd-degree Taylor polynomial at $a = 4$ to approximate $\sqrt{5}$.

- (c) If you used the same polynomial to approximate $\sqrt{6}$, would you expect your answer to be more or less accurate than it is for $\sqrt{5}$? Briefly indicate why.

2. Starting from the Taylor series at $a = 0$ for $f(x) = \sin x$, find a series for

$$\int \sin(x^2) dx.$$